- 1. (b)
- 2. (c)
- 3.

$$P_{\rm rms} = \sqrt{\int_T dt \ P^2(t)/T}$$

$$= \sqrt{\int_T dt \ (I_0 \cos(\omega t) V_0 \cos(\omega t + \theta))^2/T}$$

$$= I_0 V_0 \sqrt{\int_T dt \ [\cos(\omega t) (\cos(\omega t) \cos(\theta) - \sin(\omega t) \sin(\theta))]^2/T}$$

$$= I_0 V_0 \sqrt{\int_T dt \ [[1 - \cos(2\omega t)] \cos(\theta)/2 - \sin(2\omega t) \sin(\theta)/2]^2/T}$$

$$= (I_0 V_0 \cos(\theta)/2) \sqrt{\int_T dt \ [1 - \cos(2\omega t) - \sin(2\omega t) \tan(\theta)]^2/T}$$

$$= I_0 V_0 \cos(\theta)/2$$

4. (a)

5.

$$Z_{\text{circuit}} = \frac{1}{\frac{1}{Z} + \frac{1}{Z}} + Z + \frac{1}{\frac{1}{Z + Z} + \frac{1}{\frac{1}{\frac{1}{Z} + \frac{1}{Z}}}} = \frac{33}{14}Z$$
(1)

- 6. $Z = Z_L + Z_C + Z_R = i\omega L + 1/i\omega C + IR$, now $dZ/d\omega = iL 1/i\omega^2 C$ so set $L + 1/\omega^2 C = 0$, and find $\omega = 1/\sqrt{LC}$
- 7. $V_L(t) = I(t)Z_L = I\sin(\omega t)i\omega L$, $V_C(t) = I(t)Z_C = I\sin(\omega t)/i\omega C$, $V_R(t) = I(t)Z_R = I\sin(\omega t)R$, so we see that $\theta(V_L(t)) = \tan^{-1}(I\sin(\omega t)\omega L/0) = \tan^{-1}(\pm \infty) = \pm \pi/2$, likewise $\theta(V_C(t)) = \mp \pi/2$, and $\theta(V_R(t)) = 0$, all independent of the resonant condition.
- 8. $Z_{\text{circuit}} = R i/7\omega C$

9.
$$V_R(t) = I(t)Z_R = \frac{V_0 \sin(\omega t)}{R - i/7\omega C}R = V_0 R \sin(\omega t) \frac{R + i/7\omega C}{R^2 + 1/(7\omega C)^2}$$

 $V_{3C} = I_{3C}(t)Z_{3C} = \frac{3}{7} \frac{V_0 \sin(\omega t)}{R - i/7\omega C} \frac{1}{3i\omega C} = \frac{1}{7\omega C} V_0 \sin(\omega t) \frac{1/7\omega C - iR}{R^2 + 1/(7\omega C)^2}$

Yes, $V_{3C}(t) = V_{4C}(t)$: they are in parallel!

- 10. $\theta(V_R(t)) = \tan^{-1}\left(\frac{1}{7R\omega C}\right), \ \theta(V_{3C}(t)) = \tan^{-1}\left(-7R\omega C\right)$ 11. $a = R + 1/R((1/R^2) + (\omega C - 1/\omega L)^2), \ b = \omega L - (\omega C - 1/\omega L)/((1/R^2) + (\omega C - 1/\omega L)^2), \ \omega_{\text{resonant}} = 0$
- 12. They are both zero!
- 13. R' = R, L' = 2L/3. They are the same because the inductors are in parallel and so cannot have a different phase angle. 14. $\theta(V_L) = \tan^{-1}(3R/2\omega L)$, $\theta(V_R) = \tan^{-1}(-2\omega L/3R)$