

Problem 1.

$$\mathcal{E} = \frac{\mu_0 I b}{2\pi} \frac{2v}{a + r_0 + vt} \text{ clockwise}$$

If the loop is stationary, $\mathcal{E} = 0$. If the loop is thin it is the same as for a single rod with length b . If the loop is far away (at large t), $\mathcal{E} \rightarrow 0$.

Problem 2.

$$Q(t) = Q_+ e^{\omega_+ t} + Q_- e^{\omega_- t} \text{ for } \omega_{\pm} = \frac{-R \pm \sqrt{R^2 - 4L/C}}{2L}, Q_- = \frac{-\omega_+ Q_0}{\omega_- - \omega_+}, \text{ and } Q_+ = Q_0 + \frac{\omega_+ Q_0}{\omega_- - \omega_+}.$$

Problem 3.

Q decays exponentially from t_1 to t_2 with time constant $(R_1 + R_3)C$ and exponentially from t_2 onward with time constant $(R_3 + 1/((1/R_1) + (1/R_2)))C$. $\mathcal{E}_{R_3} = IR_3 = R_3 dQ/dt$ is a scaled version of Q (flipped from the $-$ in the exponential and scaled by R_3).

Problem 4.

$$Z_{\text{circuit}} = R + \frac{1}{\frac{1}{i\omega L} + \frac{1}{i\omega 2L}} = R + i\omega \frac{2}{3}L$$

The current through the resistor is $I(t) = I_0 \cos(\omega t)$.

The current through the inductor L as a function of time is $2I_0 \cos(\omega t)/3$.

The phase difference is always zero.