

- $P = F/A$, so $F = PA = 10^5 10^{-2} \text{ [N m}^2] = 10^3 \text{ [N]}$
- $F = PA = \int_A dA P = 10^{-2} \int_0^{0.1} dx [10^5 + 10^3 x] = 100.05 \text{ [N]}$
- $F = PA = \int_A dA P = \int_{-0.05}^{0.05} dx \int_{-0.05}^{0.05} dy [10^5 + 10^3 \cos(2\pi x/0.1) \cos(2\pi y/0.1)] = 10^3 \text{ [N]}$
- $P = P_0 + \rho gh = 10^5 + 10^3 \cdot 10 \cdot 3 = 1.3 \times 10^5 \text{ [Pa]} = 1.3 \text{ [bar]}$
- N/A
- The pressure difference between heights is equal to the pressure difference between the inside of the dewar and the atmosphere, so $4.05 \times 10^5 \text{ [Pa]} = \rho gh = 13.5 \cdot 10^3 \cdot 10h$, so $h = 3 \text{ [m]}$
- $F = F_g + F_b = -m_d g + m_w g = -\rho_d V g + \rho_w V g = (\rho_w - \rho_d) V g$. $\rho_w - \rho_d > 0$, so upwards.
- $y(t) = (\rho_w - \rho_d) g t^2 / 2 + v_0 t + y_0 = g t^2 / 2$. $y(t^*) = 20$, so $t^* = 5.16 \text{ [s]}$.
- $A_{\text{in}} v_{\text{in}} = A_{\text{out}} v_{\text{out}}$, so $v_{\text{out}} = 1000 \text{ [m/s]}$
- This is in general hard, so we assume that the engine does all of its work at $r = 0.5 \text{ [m]}$, in which case the air is moving 40 [m/s] already, then the work speeds it as $1000 = (v^2 - 40^2)^2 / 2$, or to $v = 60$, so the output speed is 1500 [m/s] .
- The area of the tube is $5.07 \times 10^{-4} \text{ [m}^2]$, so summing the flow rates, we find $v = \dot{V}/A = 0.4012 \text{ [m/s]}$

$$\dot{V}_{\text{H}_2\text{O}_2} = \frac{1 \text{ mol H}_2\text{O}_2}{1 \text{ sec}} \cdot \frac{0.034 \text{ kg H}_2\text{O}_2}{1 \text{ mol H}_2\text{O}_2} \cdot \frac{1 \text{ m}^3 \text{ H}_2\text{O}_2}{1450 \text{ kg H}_2\text{O}_2} = 2.34 \times 10^{-5} \frac{\text{m}^3}{\text{sec}}$$

$$\dot{V}_{\text{H}_2\text{O}} = \frac{10 \text{ mol H}_2\text{O}}{1 \text{ sec}} \cdot \frac{0.018 \text{ kg H}_2\text{O}}{1 \text{ mol H}_2\text{O}} \cdot \frac{1 \text{ m}^3 \text{ H}_2\text{O}}{1000 \text{ kg H}_2\text{O}} = 18 \times 10^{-5} \frac{\text{m}^3}{\text{sec}}$$

- The flow rate is now $21.6 \times 10^{-5} \text{ [m}^3/\text{s]}$ so it moves at a velocity of 0.4260 [m/s]
- $P_i + \rho g y_i + \rho v_i^2 / 2 = P_f + \rho g y_f + \rho v_f^2 / 2$, here $g y_i + v_i^2 / 2 = g y_f + v_f^2 / 2$, or with values, $v_f = 43.4 \text{ [m/s]}$
- We need to add another energy term, so: $P_i + \rho g y_i + \rho v_i^2 / 2 = P_f + \rho g y_f + \rho v_f^2 / 2 + E / [\text{m}^3]$, or $E / [\text{m}^3] = \rho g y_i + \rho v_i^2 / 2 - \rho g y_f - \rho v_f^2 / 2$, and $\dot{V} = Av$, so the power is $E \dot{V} / [\text{m}^3] = 6.21 \times 10^6 \text{ [W]}$
- We are told:

$$F_{\text{net}} = F_{\text{buoyancy}} + F_{\text{gravity}} + F_{\text{drag}}$$

So by Newton's Law:

$$m_s a = m_f g - m_s g - 6\pi\mu r v$$

Which is:

$$\left[\frac{4}{3} \pi r^3 \rho_s \right] \ddot{y} + [6\pi\mu r] \dot{y} + [0]y = \left[\frac{4}{3} \pi r^3 g (\rho_f - \rho_s) \right]$$

The roots of the characteristic equation are:

$$\lambda_{\pm} = \frac{-6\pi\mu r \pm \sqrt{(6\pi\mu r)^2 - 4 \frac{4}{3} \pi r^3 \rho_s 0}}{2 \frac{4}{3} \pi r^3 \rho_s} = -\frac{9\mu}{2r^2 \rho_s}; 0$$

Now we seek a solution to the inhomogeneous equation with form At , so:

$$\left[\frac{4}{3} \pi r^3 \rho_s \right] 0 + [6\pi\mu r] A + [0]At = \left[\frac{4}{3} \pi r^3 g (\rho_f - \rho_s) \right] \iff A = \frac{4r^2 g (\rho_f - \rho_s)}{18\mu}$$

We now apply the boundary conditions:

$$y(0) = 0 = \alpha_+ + \alpha_-$$

$$\dot{y}(0) = 0 = \alpha_+ \lambda_+ + \alpha_- \lambda_- + A$$

So we find:

$$y(t) = y_h(t) + y_p(t) = \frac{4r^4 g (\rho_f - \rho_s)}{81\mu^2} \left[\exp\left(-\frac{9\mu}{2r^2 \rho_s} t\right) - 1 \right] + \frac{4r^2 g (\rho_f - \rho_s)}{18\mu} t$$