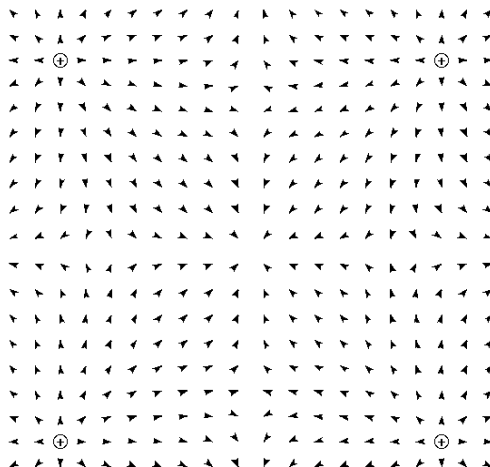


Problem 1. (15 Points)

I. (5 points)

Suppose that four stationary point charges $+Q$ are placed at the corners of a square of side length a as shown below. If a free point charge $+q$ is placed at rest somewhere in the square, at how many distinct points can it stay at rest?

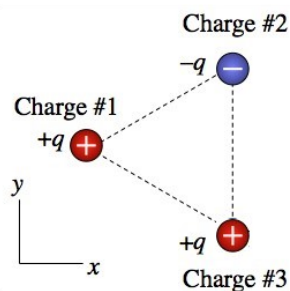
- (a) 0
- (b) 1
- (c) 2
- (d) 3
- (e) 4
- (f) 5



II. (5 points)

Three point charges lie at the vertices of an equilateral triangle as shown below. Charges 2 and 3 make up an electric dipole. The net electric force that charge 1 exerts on the dipole is in the:

- (a) $+\hat{x}$ direction
- (b) $+\hat{y}$ direction
- (c) none of the above
- (d) $-\hat{x}$ direction
- (e) $-\hat{y}$ direction



III. (5 points)

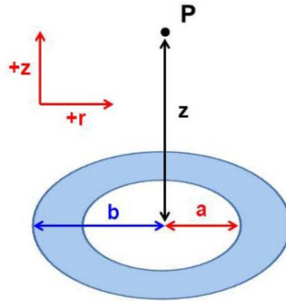
True/False questions.

- (a) Only charge enclosed within a Gaussian surface can produce an electric field at points on the Gaussian surface. (3 points)
- (b) If there is no net charge inside of a Gaussian surface, the electric field must be zero at all points on the Gaussian surface. (2 points)

Problem 2. (30 Points)

An annulus has inner radius a and outer radius b and carries a uniform charge density of σ .

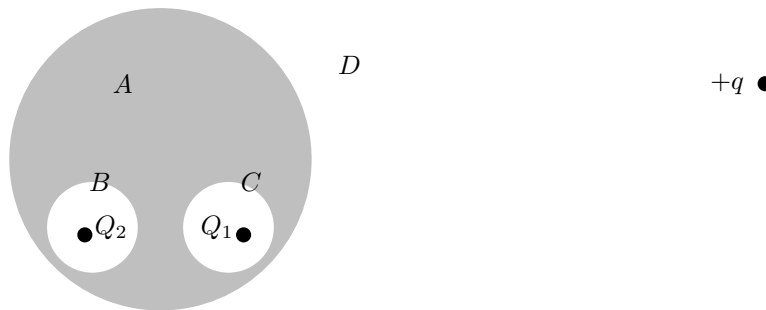
- Calculate the electric potential V at point P , a distance z above the origin on the positive z -axis. (15 points)
- Using $\mathbf{E} = -\nabla V$, calculate the electric field at point P from the electric potential V . (10 points)
- What is the electric field at P for a uniformly charged disk of radius R ? (5 points)



Problem 3. (20 Points)

Two off-centered cavities are located inside a spherical conductor. Two off-centered point charges $+Q_1$ and $+Q_2$ are located inside these cavities as shown.

- Qualitatively, draw the surface charge distributions and electric field lines at A, B, C and D . (10 points)
- A point charge $+q$ is placed outside the conductor a distance r from the center of the conductor, a distance r_1 from charge Q_1 and a distance r_2 from charge Q_2 ($r \gg$ the radius of the spherical conductor). What is the total force acting on the point charge $+q$? (10 points)



Problem 4. (35 Points)

A hollow insulating spherical shell of inner radius R_0 and outer radius R_1 carries a charge density of $\rho(r) = \rho_0(r/R_1)^3$. A positive charge $+Q$ is placed in the center of the hollow spherical shell and a grounded conducting shell with inner radius R_2 and outer radius R_3 surrounds the hollow sphere.

- What is the total charge on the insulating spherical shell? (5 points)
- What charges are on the inner and outer surfaces of the conducting shell? (5 points)
- Find the electric field at all points in space. (15 points)
- Plot the electric field as a function of r . (5 points)
- How would change if the conducting shell was not grounded (and was not given any charge)? (5 points)

