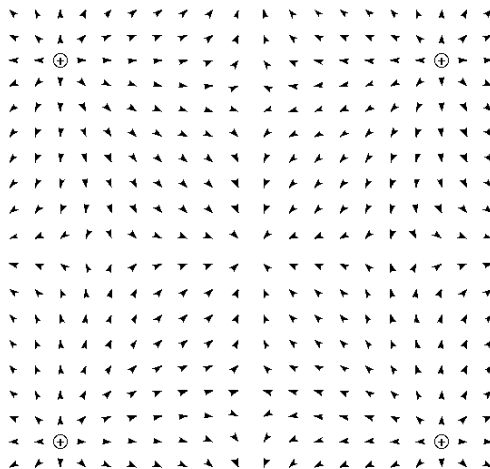


Problem 1. (15 Points)
I. (5 points)

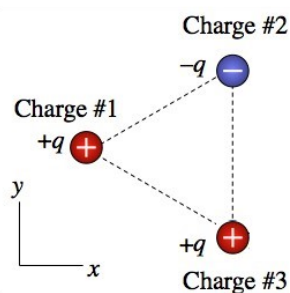
Suppose that four stationary point charges $+Q$ are placed at the corners of a square of side length a as shown. If a free point charge $+q$ is placed at rest somewhere in the square, at how many distinct points can it stay at rest?

- | | |
|-------|-------|
| (a) 0 | (d) 3 |
| (b) 1 | (e) 4 |
| (c) 2 | (f) 5 |


II. (5 points)

Three point charges lie at the vertices of an equilateral triangle as shown. Charges 2 and 3 make up an electric dipole. The net electric force that charge 1 exerts on the dipole is in the:

- | | |
|--------------------------|--------------------------|
| (a) $+\hat{x}$ direction | (d) $-\hat{x}$ direction |
| (b) $+\hat{y}$ direction | (e) $-\hat{y}$ direction |
| (c) none of the above | |


III. (5 points)

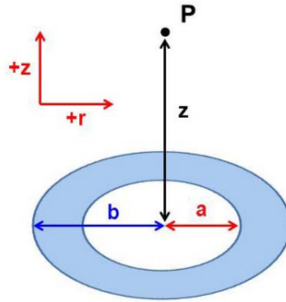
True/False questions.

- If there is no net charge inside of a Gaussian surface, the electric field must be zero at all points of that surface. (2 points)
- Only charge enclosed within a Gaussian surface can produce an electric field at points on that surface. (2 points)
- If there is no field in the area, there is also no charge in that area. (1 point)

Problem 2. (30 Points)

An annulus of radii between a and b has a uniform charge density of σ .

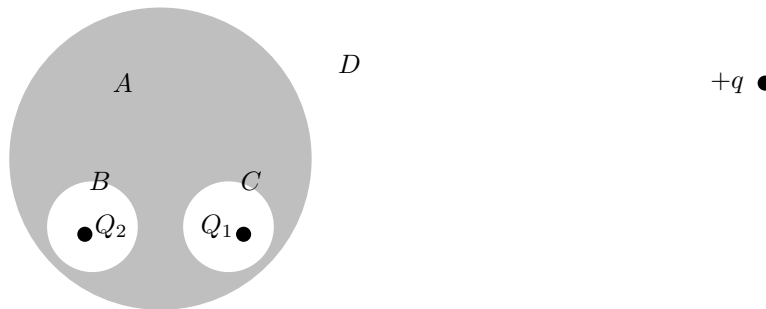
- Calculate the potential at point P , a distance z on the positive z -axis. (15 points)
- Using $\mathbf{E} = -\nabla V$, calculate the electric field at point P from the potential. (10 points)
- Take a suitable limiting approximation to estimate the electric field at P for a uniformly charged disk of radius R , (5 points)



Problem 3. (20 Points)

Two off-centered cavities are located inside a spherical conductor. Two off-centered point charges $+Q_1$ and $+Q_2$ are located inside these cavities as shown.

- Please plot the surface charge distributions and representative electric field lines in space A, B, C and D (10 points)
- A point charge $+q$ is placed outside the conductor a distance r from the center of the conductor, a distance r_1 from charge Q_1 and a distance r_2 from charge Q_2 ($r \gg$ the radius of the spherical conductor). What is the total force acting on the point charge $+q$? (10 points)



Problem 4. (35 Points)

A hollow insulating spherical shell of inner radius R_0 and outer radius R_1 is positively charged with a charge density of $\rho(r) = \rho_0(1 - (r/R_1)^3)$. A positive charge $+Q$ is placed in the center of the hollow sphere and a concentric grounded conducting shell with inner radius R_2 and outer radius R_3 surrounds the hollow sphere. (The conducting shell was neutral before it is grounded.)

- What is the total charge on the insulating sphere? (5 points)
- What charges are on the inner and outer surfaces of the conducting shell? (5 points)
- Find the electric field at all points in space; plot this as a function of r . (20 points)
- What about your answers for (a) and (b) would be different if the conducting shell was not grounded (and was not given any charge)? (5 points)

